



**AVANTHI INSTITUTE OF ENGINEERING AND TECHNOLOGY**  
Tamaram, Makavarapalem, Visakhapatnam-531113

**CIRCULAR**

**Ref:AIET/Internal Exams/Revaluation/January 2021**

**Date: 05-02-2021**

**Attn: II BTECH-ISEMESTER STUDENTS**

**ANNOUNCEMENT OF MID-1 MARKS**

All the students of II B.Tech I Semester are hereby informed that mid-I scripts valuation is completed and internal marks are tabulated. The same are displayed in the department notice board. Go through your marks and if any discrepancy is observed, approach your Head of the Department with a written request by 07-02-2021.

No request for verification of marks is allowed after cut off date.

  
**Principal**  




Visakhapatnam,

Dt: 06/02/2021

To,

The Head Of The Department,  
Avanathi Institute Of Engg and Technology,  
Makavarapalem.

Respected Sir,

sub: Request for reevaluation

I am D. Gopal Raju of ECE department  
studying in II B.Tech I semester bearing roll number  
19811A0415

Sir, I am not satisfied with the internal  
marks I have attained for the subject RVSP.  
So, I request you to kindly reevaluate my  
internal marks


Thanking You Sir

Yours Obediently

D. Gopal Raju

19811A0415

forward to T.P. Naidu  
ECE depart  
verify & check the internal  
marks of RVSP.

  
HOD ECE



Visakhapatnam,

Dt: 07/02/2021

To

The Head of the Department,  
Avanathi Institute of Engg and Technology,  
Makavarapalem.

Respected Sir,

Sub: Request for revaluation.

I am A. Padmini Prasanthi of ECE  
Department studying in II B.Tech I Semester  
bearing roll number 20815A0403

Sir, I am not satisfied with the  
internal marks I have attained for the subject  
RVSP.

So, I request you to kindly revaluate  
my internal marks.

Thanking you Sir,

Yours obediently,  
A. Padmini Prasanthi.

Forward to  
TIP made  
checked & verified

  
HOD, ECE





# AVANTHI INSTITUTE OF ENGINEERING & TECHNOLOGY

Tamaram, Makavarapalem, Narsipatnam Revenue Division, Visakhapatnam Dist-531113.

Add. Code No. **E**

Total Marks

**14/1=15**  
**20**

## MAIN ANSWER SHEET

MID EXAMINATION - I / II / III / IV Semester: I / II / III / IV / V

COURSES : B.Tech / MBA / M.Tech.

Q.No.	Section A			Section B	
	1	2	3	4	5
Marks					

Name..... **D. GOPAL RAJU** ..... Subject:..... **RVSP** ..... Date... **30/01/21** .....

Year & Branch... **2nd E.C.E.** No. of Additional... **02** ..... Roll No. **19811A0415**

Signature of the Invigilator : **[Signature]**

Q.1.a) Cumulative distribution function:- The cumulative distribution function is have a random variable  $x$ , when it is defined the probability. Then the random variable ' $x$ ' is have "less than or equal to 1".

$$f_x(x) = P(X \leq x)$$

\* Properties:-

1) If the cumulative distribution function (CDF) is defined as  $f_x(x) = P(X \leq x)$ , the random variable  $x$  lies between 0 and 1

2)  $f(-\infty) = 0$  and  $f(\infty) = 1$ .

3)  $f(x_1) \leq f(x_2)$ , this condition the CDF is non-decreasing function.

4)  $f(x_1) \leq x \leq f(x_2)$ ;  $f(x_1) = f(x_2)$ , so, we can find  $x$  is a random variable.

5) If the <sup>function</sup>  $f_x(x)$  is a random variable ' $x$ ' value is

$$f_x(x) = x_1 < x_2 \text{ --- } x_{i-1} < x_i \text{ is written by}$$

$$P(X \leq x) \times P(X > x) = 5$$



hence,  $P(X \leq x) \cup P(X > x) = P(S) = 1$

6)  $f(x_1) \leq x \leq f(x_2)$ ;  $f(x_1) \neq f(x_2)$ , the random variable  $x$  is equal.

7) The random variable  $x$  is discrete function then we can write

$f_x(x) = P(X \leq x) < P(X < x)$  written in mathematical form

$$f_x(x) = \sum_{i=0}^{\infty} P(x_{i-1}) + P(x_i)$$

$$f_x(x) = \begin{cases} 1, & x_1 \leq x < x_2 \text{ unit step distribution.} \\ 0 & \text{else.} \end{cases}$$

1b) Given  $f_x(x) = \int_{-\infty}^{\infty} \frac{e^{-\frac{(x-\mu)^2}{2\sigma^2}}}{\sqrt{2\pi}\sigma} e^{-\frac{(x-\mu)^2}{2\sigma^2}} dx$

$\mu_x = 2$  and  $\sigma_x = 2$

i) Find  $P\{x > 1.0\} = P(f_x(x) > 1.0) = 1 - P(f_x(x) \leq 1.0) = 1 - P(-1.5) = Q(1.5)$

Here  $Q(x) = \left[ \frac{1}{0.699(x) + 0.388(x+5.81)} \right] e^{-\frac{x^2}{2\pi}}$

$Q(1.5) = \left[ \frac{1}{0.699(1.5) + 0.388(1.5+5.81)} \right] e^{-\frac{(1.5)^2}{2\pi}}$

$Q(1.5) = 0.0688$

$\therefore P\{x > 1.0\} = 0.0688$



$$ii) P\{x \leq -1.0\} = P\{f(x)\} = 1 - P\{f(x)\}$$

$$= 1 - P(-1.0)$$

$$P = 0.5$$

$$\therefore Q = 0.5$$

$$\text{Here } Q(x) = \left[ \frac{1}{0.699(x) + 0.388(x+5.51)} \right] e^{-\frac{x^2}{2}}$$

$$Q(-0.5) = \left[ \frac{1}{0.699(-0.5) + 0.388(-0.5) + 5.51} \right] e^{-\frac{(-0.5)^2}{2}}$$

$$= -0.03881 = 1 - P(x) = 1 - P(0.03881)$$

$$\therefore P\{x \leq -1.0\} = -0.6915 = -0.6915$$

02)  
b)

Given

$f_2(x)$	0	1	2	3	4	5
$x$	$1/32$	$5/32$	$10/32$	$10/32$	$5/32$	$1/32$

The ~~distribution~~ <sup>mean</sup> of probabilities is

$$f_x(x) = \sum_{i=0}^5 P(x_i) \cdot x_i$$

$$= 0 \cdot \frac{1}{32} + 1 \cdot \frac{5}{32} + 2 \cdot \frac{10}{32} + 3 \cdot \frac{10}{32} + 4 \cdot \frac{5}{32} + 5 \cdot \frac{1}{32}$$

$$= 2.5$$

The variance of the probabilities.

$$f_x(x) = P(x_i - \bar{x}) \cdot P(x_i)$$

$$= 0 \times \frac{1}{32} + 1 \times \frac{5}{32} + 2 \times \frac{10}{32} + 3 \times \frac{10}{32} + 4 \times \frac{5}{32} + 5 \times \frac{1}{32}$$

$$= (0-2.5) \times \frac{1}{32} + (1-2.5) \times \frac{5}{32} + (2-2.5) \times \frac{10}{32} + (3-2.5) \times \frac{10}{32} + (4-2.5) \times \frac{5}{32} + (5-2.5) \times \frac{1}{32}$$



$$= \frac{1}{32} [6 \cdot 25 + 11 \cdot 2 + 10 + 10 + 11 \cdot 2 + 6 \cdot 25]$$

$$= \frac{85}{32}$$

Q3a) Given  $f_{xy}(x,y) = \begin{cases} b(x+y)^2 & -2 < x < 2 \text{ and} \\ 0 & \text{else where.} \end{cases}$

The function is

$$f_{xy}(x,y) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} b(x+y)^2 dx dy$$

$$= \int_{-2}^2 \int_{-3}^3 b(x+y)^2 dx dy$$

$$= \int_{-2}^2 \int_{-3}^3 b(x^2 + y^2 + 2xy) dx dy$$

$$= b \int_{-2}^2 \int_{-3}^3 (x^2 + y^2 + 2xy) dx dy$$

Integration is respectively

$$= b \int_{-2}^2 \left[ x^2 + \frac{x^3}{3} + x^2 y + \frac{y^2}{3} \right]_{-3}^3 dx dy$$

$$= b \int_{-2}^2 [3x^2 + 9x + 9 + b \int_{-3}^3 [3x^2 - 9x - 9]] dx dy$$

$$= b \int_{-2}^2 (6x - 18x^2) dx dy$$

$$= 6b \int (x - 3x^2) dx dy$$

$$= 6b \int \left( \frac{1}{2}x^2 - x^3 \right) dx dy$$





# ADDITIONAL ANSWER SHEET

Subject : RVS P

Signature with Date : Prak  
30/11

$$= 12b \int \frac{1}{(12)(12b)} dx dy$$

$$\therefore b = \frac{1}{104}$$

ii) The marginal density function of  $f_x(x)$

$$f_x(x) = \int_{-\infty}^{\infty} b(x+y)^2 dy$$

$$= \int_{-3}^3 \frac{1}{104} (x+y)^2 dy$$

$$= \frac{1}{312} [(3x+1) + (3x-1)] dx$$

$$\therefore f_x(x) = \frac{1}{312} [(3x+1) + (3x-1)] dx$$

The marginal density function of  $f_y(y)$

$$f_y(y) = \int_{-\infty}^{\infty} b(x+y)^2 dx$$

$$= \int_{-2}^2 \frac{1}{104} (x+y)^2 dx$$

$$= \frac{1}{312} [(2y+1) + (2y-1)] dy$$

$$\therefore f_y(y) = \frac{1}{312} [(2y+1) + (2y-1)] dy$$

03b) Given random variable  $f(x) = ae^{-bx}$

ii) The a and b are real constants

$$f_x(x) = \int_{-a}^0 e^{tx} dx + \int_a^{\infty} e^{-tx} dx$$



$$= \int_{-a}^0 a e^{tx} f(x) dx + \int_a^{-a} a e^{-tx} f(x) dx$$

$$= a \int_{-a}^0 e^{tx} (b+t) dx + \int_a^{-a} a e^{-tx} (b-a) dx$$

$$= a \int_{-a}^0 e^{tx} (b+t) dx + \int_a^{-a} e^{-tx} (b-t) dx$$

$$= a \left[ \int_{-a}^0 \frac{e^{(b+t)x}}{b+t} dx + \int_a^{-a} \frac{e^{-(b-t)x}}{b-t} dx \right]$$

$$= a \left[ \frac{1}{b+t} + \frac{1}{b-t} \right] dx$$

$$= a \left[ \frac{b+t+b-t}{(b+t)(b-t)} \right] dx$$

$$= \frac{2ab}{b^2}$$

$$\therefore m_x = \frac{2ab^2}{b^3}$$

ii) mean

$$\Rightarrow f(x) = 2ab \int (b-t) dx \Big|_{t=0} = 2ab \int (b-t) dx \Big|_{t=0}$$

$$= 2ab \int (b-t) + (b-2x) dx \Big|_{t=0}$$

$$= 2ab \int_0 dx$$

$$m_x = 0$$





## ADDITIONAL ANSWER SHEET

Subject : RVSP

Signature with Date : Keala  
30/1/21

Moment generating function

$$f(x) = 2ab \int (b-t) f(x) dx \quad \text{at } t=0$$

$$= 2ab \int (b-t) f(x) dx \quad \text{at } t=1$$

$$= 2ab \int (b-t) dx - (2x) dx \quad \text{at } t=1$$

$$= \frac{4a}{b^3}$$

$$\sqrt{x} = 2ab \int (b-t)$$

$$= \frac{4a}{b^3}$$

$$\therefore \sqrt{x} = \frac{4a}{b^3}$$

2) The properties of variance :-

a) i) If the variance is constant  $x$ , then the constant variable  $k$  is zero value.  $a=0$ proof

$$\text{Var}(x) = \int (x - mx) dx$$

$$= [E - m(x)] dx$$

$$= [E - m(0)] dx$$

$$= 0$$

$$\therefore \text{Var}(x) = 0$$

ii) If the variance is constant  $k$ , then we can find the ~~red~~ constant variable.



proof:  $\text{Var}(kx) = \text{Var}[E - k(x)] dx$

$$= [E^2 - k^2(x)^2] dx$$

$$= \int [E^2 - k^2(x)^2] dx$$

$$= \int [E^2 - (kx)^2] dx =$$

$$\therefore \text{Var}(kx) = [E^2 - (kx)^2] dx$$

iii) the random variable  $x$  is constant, then we can find the real constant variable.

proof

$$\text{Var}(kx)^2 = \text{Var}([E(ax+b)^2 + E(ax-b)^2]) dx$$

$$= [E - (ax+b)^2 + E(ax-b)^2] dx$$

$$= [E(a^2 + b^2 + 2ab)x + E(a^2 + b^2 - 2ab)x] dx$$

$$= [E - (a^2 + b^2 + 2abx) + (a^2 + b^2 - 2abx)] dx$$

$$= [E - (a^2 + b^2) + (a^2 - b^2)] dx$$

$$= [E - (a+b)^2 + (a-b)^2] dx$$

$$\therefore \text{Var}(kx) = [E - (a+b)^2 + (a-b)^2] dx$$





# AVANTHI INSTITUTE OF ENGINEERING & TECHNOLOGY

Add. Code No.

Tamaram, Makavarapalem, Narsipatnam Revenue Division, Visakhapatnam Dist-531113.

Total Marks

11  
20

## MAIN ANSWER SHEET

MID EXAMINATION - I / II / III / IV Semester: I / II / III / IV / V

COURSES : B.Tech / MBA / M.Tech.

Q.No.	Section A			Section B	
	1	2	3	4	5
Marks	10				

Name: A. Padmini Pavananthi Subject: RVSP Date: 30-01-21

Year & Branch: 2<sup>nd</sup> ECE No. of Additional: - Roll No. 20815A0403

Signature of the Invigilator: *[Signature]*

1) a) properties of cumulative distribution function:

1.  $f(x)$  is a non decreasing function then

$$f(x) = F(x_1) - F(x_2)$$

2)  $f(x) \cdot f(x) - \alpha = 0$

All the real numbers will be from  $-\infty$  to  $\infty$ . There are no real numbers less than  $-\infty$ . As we know that definition of cumulation  $f(x) = P(x \leq \infty)$

3)  $f(x) + \infty = 1$

As per the definition  $f(x) = P(x \leq -\infty) = 1$

So, all the real values and probabilities of the function are given in a sample space is always equals to one.

4)  $0 < f(x) \leq 1$ . Here  $F(x)$  is a also a probability distribution function.

5) If we are taking the  $x_1, x_2, x_3$  where  $x_1 < x_2 < x_1 - x < x_3$ . then

$$F(x) = P(x - x) - (x_1 - x)$$



$$b) (i) P\{x > 1.0\} = 1 - f_x(x).$$

$$= f_x(x) - 1.$$

$$= \left(\frac{1-2}{2}\right) = 0.5 \quad 1 - f(x) = \frac{1 - 0.5}{\sqrt{2\pi}}$$

$$= \theta(0.5).$$

$$\theta(x) = \frac{1}{0.333(x) + 0.399 \sqrt{x^2 + 5.51}} \cdot \frac{x^{-2/2}}{\sqrt{2\pi}}$$

$$= \theta(0.5) = \frac{1}{0.33(0.5) + 0.399 \sqrt{(0.5)^2 + 5.51}} \cdot \frac{x^{-0.5/2}}{\sqrt{2\pi}}$$

$$= 0.308.$$

$$P\{x > 1.0\} = 1 - f_x(x).$$

$$= 1 - \theta(x)$$

$$= 1 - 0.308$$

$$= 0.6915.$$

$$(ii) P\{x \leq 1.0\} = 1 - f_x(x)$$

$$= 1 - (-1.5).$$

$$= f(x) F_x x(1.5)$$

$$= \theta(1.5).$$

$$\theta(x) = \frac{1}{0.333(x) + 0.399 \sqrt{x^2 + 5.51}} \cdot \frac{x^{-2/2}}{\sqrt{2\pi}}$$

$$\theta(1.5) = \frac{1}{0.333(1.5) + 0.399 \sqrt{1.5^2 + 5.51}} \cdot \frac{x^{-1.5/2}}{\sqrt{2\pi}}$$

$$= 0.0668.$$



$$P\{x \leq 1.0\} = 1 - F_X(x)$$

$$= 1 - F_X(1.0)$$

$$= 1 - 0.9332$$

$$= 0.0668$$

2) a)

Properties of variance:

1) The constant 'k' of 'x' is  $\left(\frac{0}{1}\right)$  i.e.  $\left(\frac{1}{1}\right)$  k is a constant then  $k(x) = 0$ .

$$\therefore \boxed{k(x) = 0}$$

2) If variance of x is a function of  $E(x)$  then constant k. i.e.

$$\text{Var} f(x) = k^2 + bx$$

3) If  $\left(\frac{0}{k}\right)$  is constant and a and b are two real numbers then

$$\text{Var}(ax + b) = a^2 + bx$$

4) If a and b are two identical real numbers then

$$\text{Var}[a(x) + b(x)] = \text{Var}[a(x)] + \text{Var}[b(x)]$$

$$\text{Var}[a(x) - b(x)] = \text{Var}[a(x)] + \text{Var}[b(x)]$$



b)	x	0	1	2	3	4	5
	p(x)	1/32	5/32	10/32	10/32	5/32	1/32

As we know that

$$\text{mean } E(x) = \sum x_i P(x_i)$$

$$= 0 \left( \frac{1}{32} \right) + 1 \left( \frac{5}{32} \right) + 2 \left( \frac{10}{32} \right) + 3 \left( \frac{10}{32} \right) + 4 \left( \frac{5}{32} \right) + 5 \left( \frac{1}{32} \right)$$

$$= 2.5$$

Variance of this probability distribution function:

$$= \sum_{i=1}^n E(x - x_i)^2 P(x_i - x_i^2)$$

$$= (0 - 2.5)^2 \left( \frac{1}{32} \right) + (1 - 2.5)^2 \left( \frac{5}{32} \right) + (2 - 2.5)^2 \left( \frac{10}{32} \right) +$$

$$(3 - 2.5)^2 \left( \frac{10}{32} \right) + (4 - 2.5)^2 \left( \frac{5}{32} \right) + (5 - 2.5)^2 \left( \frac{1}{32} \right)$$

$$= 1.25$$

mean of the probability distribution =

$$2.5$$

variance of the probability distribution

$$\text{Function} = 1.25$$